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BHASKARA'S CALCULATIONS OF THE GNOMON'S SHADOW

BY

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The following problems, proposed and solved by Bhaskara in his Siddhantasiromani, are characteristic of his work.

(i) To find the gnomon's shadow in a given direction on any day in a place of known latitude.

Bhaskara's formula runs as follows:

पलप्रभा व्यासद्ळेन निष्ठी दिग्ज्योद्भृता तां पलभां प्रकल्प्य साध्याक्षजीवाथ तया विनिष्ठी स्वाक्षज्यपाप्तापमाशिज्ञिनी च॥ ताभ्यां दिनार्थेद्युतिवद्विद्ध्यादभीष्टादिक्स्थे द्यमणौ द्युतिं वा।

that is, assuming Rs/sin a to be the equinoctial shadow where s is the original equinoctial shadow, R the radian measured in minutes and equal to 3438 and a the azimuth of the moment, compute the sine of the corresponding latitude, say $\sin L$; then compute $\sin D$ from the formula $\sin D = \sin d \sin L/\sin \varphi$ where d is the sun's declination and φ the latitude of the place. Then $L \pm D$ gives us the zenith-distance wherefrom the shadow can be derived,

The equinoctial shadow is that cast by the gnomon on an equinoctial day at noon. Thus $s/12 = \tan \varphi$, the gnomon's length being 12 units. Hence the Hindu sine of the latitude of the place, in terms of the equinoctial shadow would be $\frac{Rs}{\sqrt{12^2+s^2}}$ where the Hindu sine is the modern sine multiplied by R.

The formula may be proved as follows according to modern methods.

Let TRQ be the equator, Z the zenith, P the pole and S the Sun's position. ZS, the zenith-distance of the Sun is equal to ZT±ST according as the Sun is in the South or North of the Equator. ZT

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